

Convergence Analysis of the Filtered-x LMS Adaptive Algorithm for Active Noise Control System

Kang-Seung Lee* Regular Member

ABSTRACT

Application of the Filtered-X LMS adaptive filter to active noise control requires to estimate the transfer characteristics between the output and the error signal of the adaptive canceler. In this paper, we derive an adaptive control algorithm and analyze its convergence behavior when the acoustic noise is assumed to consist of multiple sinusoids. The results of the convergence analysis of the Filtered-X LMS algorithm indicate that the effects of parameter estimation inaccuracy on the convergence behavior of the algorithm are characterized by two distinct components: Phase estimation error and estimated magnitude. In particular, the convergence of the Filtered-X LMS algorithm is shown to be strongly affected by the accuracy of the phase response estimate. Simulation results of the algorithm are presented which support the theoretical convergence analysis.

I. INTRODUCTION

Adaptive approaches have widely been used in active noise control applications in which the unwanted noise sound is adaptively synthesized with the equal amplitude but opposite phase, resulting in the control of the acoustic noise as shown in Fig. 1.

In Fig. 1, the input microphone can be replaced by other non-acoustical sensors such as tachometers or accelerometers in which case the possibility of the speaker output feedback to the input microphone is removed [1]. For instance, periodic noises to be cancelled can be generated using its fundamental sinusoid. The adaptive filter output drives the loudspeaker in such a way that the acoustic noise and the loudspeaker output can be summed to null at the error microphone.

Although any adaptive algorithm can be used in Fig. 1 is not appropriate. The reason is that the acoustic path between the filter output and summation point of the error signal is frequency sensitive, which acts to distort the phase and magnitude of the error signal. In turn, the distortion of the phase and magnitude in the error path can degrade the convergence performance of the LMS algorithm. As a result the convergence rate is lowered, the residual error is increased, and the algorithm can even become unstable. For these reasons, it is necessary to use the so-called Filtered-x LMS algorithm [2,3,4,5,6] for which the transfer characteristics between the output and the error signal of the adaptive canceler must be estimated and the result be used in the adaptive algorithm.

* Dept. of Computer Engineering, DongEui University(kslee@dongeui.ac.kr)
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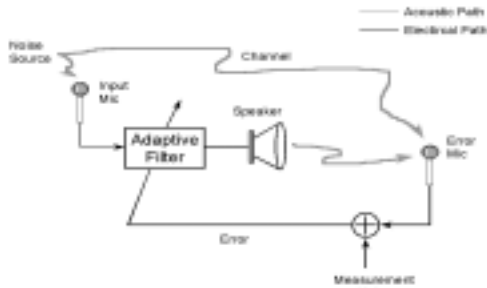


Fig. 1. Basic adaptive active noise controller configuration.

In many practical applications, the acoustic noise to be cancelled is generated by rotation machines and thus can be modeled as the sum of a fundamental sinusoid and its harmonics [2,3,7,11]. For example, fan noise is frequently generated in the consumer electronic products such as air conditioners, vacuum cleaners and so on. In this paper we are concerned with cancellation of fan noise based on active noise control filtering. And we derive an adaptive controller structure and analyze its convergence behavior when the acoustic noise can be modeled as the sum of a fundamental sinusoid and its harmonics [2,3,7,8,11]. The convergence analysis is focused on the effects of parameter estimation inaccuracy on the performance.

Following the introduction, we give a brief description of the underlying system model in Section II. The results of the convergence analysis and the simulation are presented in Sections III and IV, respectively. Finally we make a conclusion in Section V.

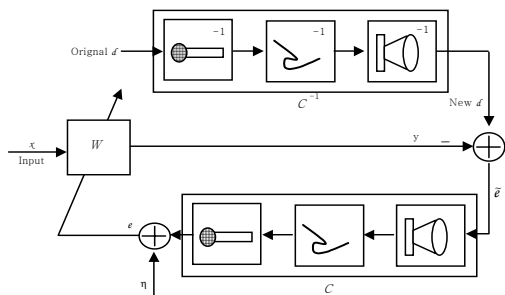


Fig. 2. Rearranged form of the controller under linear system condition.

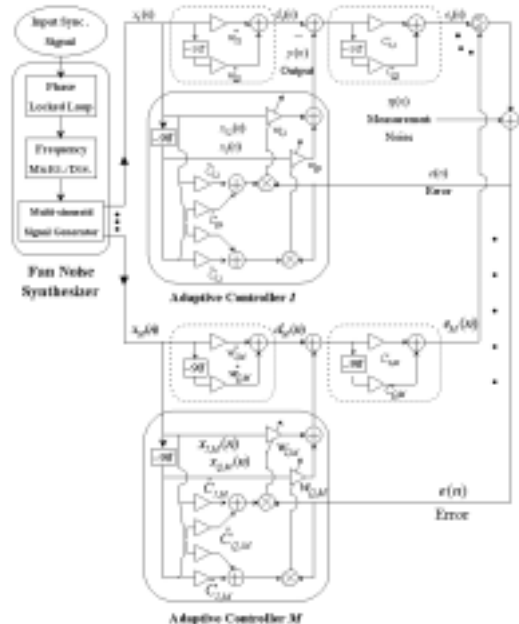


Fig. 3. The diagram of adaptive active noise control system under study.

II. SYSTEM MODEL

Since the loud speaker-air-microphone path of Fig. 1 is linear, one can easily get the equivalent system as shown in Fig. 2. When the noise consists of the multiple sinusoids only, the acoustic and loudspeaker-acoustic-microphone paths can be described by the multiple in-phase (I) and quadrature (Q) weights as shown in the upper branch of Fig. 3. For the m -th sinusoidal noise the adaptive canceler structure also becomes to have two weights $\omega_{I,m}(n)$ and $\omega_{Q,m}(n)$, with I and Q inputs, $x_{I,m}(n)$ and $x_{Q,m}(n)$, respectively. Thus the output of the m -th canceler, $y_m(n)$, is expressed as

$$y_m(n) = \omega_{I,m}(n)x_{I,m}(n) + \omega_{Q,m}(n)x_{Q,m}(n) \quad (1)$$

where

$$x_{I,m}(n) = A_m \cos(\omega_m n + \varphi_m) \triangleq A_m \cos \Psi_m(n),$$

$$x_{Q,m}(n) = A_m \sin(\omega_m n + \varphi_m) \triangleq A_m \sin \Psi_m(n),$$

m : branch index = 1, 2, 3, ..., M ,

n : discrete time index,

A : amplitude,
 ω_m : normalized frequency,
 Ψ_m : random phase.

Also, referring to the notation in Fig. 2, the error signal $e(n)$ is represented by

$$\begin{aligned} e(n) &= \sum_{m=1}^M [c_{I,m} \tilde{e}_{I,m}(n) + c_{Q,m} \tilde{e}_{Q,m}(n)] + \eta(n) \\ &= - \sum_{m=1}^M [A_m \{c_{I,m} \cos \Psi_m(n) + c_{Q,m} \sin \Psi_m(n)\} \\ &\quad \{\omega_{I,m}(n) - \omega_{I,m}^*\}] \\ &\quad - \sum_{m=1}^M [A_m \{c_{I,m} \sin \Psi_m(n) + c_{Q,m} \cos \Psi_m(n)\} \\ &\quad \{\omega_{Q,m}(n) - \omega_{Q,m}^*\}] + \eta(n) \end{aligned} \quad (2)$$

where

$$\tilde{e}_I(n) \triangleq \tilde{e}(n) = \sum_{m=1}^M \{d_m(n) - y_m(n)\},$$

\tilde{e}_Q : 90° phase-shifted version of \tilde{e}_I

$\eta(n)$: zero-mean measurement noise.

Assuming that $\omega_{I,m}(n)$ and $\omega_{Q,m}(n)$ are slowly time-varying as compared to $x_{I,m}(n)$ and $x_{Q,m}(n)$, the phase-shifted output is given from (1) by

$$\begin{aligned} y_{Q,m}(n) &= \sum_{m=1}^M \{\omega_{I,m}(n) x_{Q,m}(n)\} \\ &= \sum_{m=1}^M A_m \{\omega_{I,m}(n) \sin \Psi_m(n) - \omega_{Q,m}(n) \cos \Psi_m(n)\}. \end{aligned} \quad (3)$$

From (1), (2), and (3), one can obtain as LMS weight update equation by minimizing $e^2(n)$ and using a gradient-descent method [4] as

$$\begin{aligned} \omega_{I,m}(n+1) &= \omega_{I,m}(n) + \mu e(n) \{c_{I,m} x_{I,m}(n) + c_{Q,m} x_{Q,m}(n)\}, \\ \omega_{Q,m}(n+1) &= \omega_{Q,m}(n) + \mu e(n) \{c_{I,m} x_{Q,m}(n) - c_{Q,m} x_{I,m}(n)\}, \end{aligned} \quad (4)$$

where $m=1,2,\dots,M$ and μ is a convergence constant.

It is noted that to implement the filtered-x LMS algorithm of (4), the values of c_I and c_Q must be estimated [10]. In the following, we analyze the effects of replacing $c_{I,m}$ and $c_{Q,m}$ in (4) with $\hat{c}_{I,m}$ and $\hat{c}_{Q,m}$ on the convergence behavior of the canceler.

III. CONVERGENCE ANALYSIS

A. The mean of weight error (Magnitude)

To see how the adaptive algorithm derived in (4) converges for inaccurate $\hat{c}_{I,m}$ and $\hat{c}_{Q,m}$, we first investigate the convergence of the expected values of the adaptive weights. From the underlying signal model (Fig. 2), $E[\omega_{I,m}(n)]$ and $E[\omega_{Q,m}(n)]$ are expected in the steady state to have $\omega_{I,m}$ and $\omega_{Q,m}$ respectively. To simplify the convergence equation, we may introduce two weight errors as

$$v_{I,m}(n) \triangleq \omega_{I,m}(n) - \omega_{I,m}$$

$$\text{and } v_{Q,m}(n) \triangleq \omega_{Q,m}(n) - \omega_{Q,m}. \quad (5)$$

Then, from (2), (5) and Fig. 2, we get

$$\begin{aligned} \tilde{e}_{I,m}(n) &= -v_{I,m}(n) x_{I,m}(n) - v_{Q,m}(n) x_{Q,m}(n), \\ \tilde{e}_{Q,m}(n) &= -v_{I,m}(n) x_{Q,m}(n) + v_{Q,m}(n) x_{I,m}(n). \end{aligned} \quad (6)$$

Inserting (5) into (4), we have

$$\begin{aligned} v_{I,m}(n+1) &= v_{I,m}(n) + \mu_m e(n) \{\hat{c}_{I,m} x_{Q,m}(n) + \hat{c}_{Q,m} x_{Q,m}(n)\}, \\ v_{Q,m}(n+1) &= v_{Q,m}(n) + \mu_m e(n) \{\hat{c}_{I,m} x_{Q,m}(n) - \hat{c}_{Q,m} x_{I,m}(n)\}. \end{aligned} \quad (7)$$

Rearranging (7) with (2) and (6), taking expectation both sides of the resultant two weight error equations, we can get the following convergence equation based on the independent assumption on the underlying signals; $x_m(n)$, $\eta(n)$, $v_{I,m}$ and $v_{Q,m}$. That is,

$$\begin{pmatrix} E[v_{I,m}(n+1)] \\ E[v_{Q,m}(n+1)] \end{pmatrix} = \begin{pmatrix} \alpha_m & \beta_m \\ -\beta_m & \alpha_m \end{pmatrix} \begin{pmatrix} E[v_{I,m}(n)] \\ E[v_{Q,m}(n)] \end{pmatrix} \quad (8)$$

where

$$\alpha_m \triangleq 1 - \frac{1}{2} \mu_m A_m^2 (c_{I,m} \hat{c}_{I,m} + c_{Q,m} \hat{c}_{Q,m})$$

$$\beta_m \triangleq \frac{1}{2} \mu_m A_m^2 (\hat{c}_{I,m} c_{Q,m} - c_{I,m} \hat{c}_{Q,m}).$$

Here, defining gain and phase response parameters as

$$g_m \triangleq \sqrt{c_{I,m}^2 + c_{Q,m}^2},$$

$$\hat{g}_m \triangleq \sqrt{\hat{c}_{I,m}^2 + \hat{c}_{Q,m}^2},$$

$$\theta_{c,m} \triangleq \tan^{-1} \left(\frac{c_{Q,m}}{c_{I,m}} \right),$$

$$\text{and } \theta_{\hat{c},m} \triangleq \tan^{-1} \left(\frac{\hat{c}_{Q,m}}{\hat{c}_{I,m}} \right).$$

α_m and β_m in (8) can alternatively be expressed as

$$\alpha_m \triangleq 1 - \frac{1}{2} \mu_m A_m^2 g_m \hat{g}_m \cos \Delta \theta_{c,m}$$

$$\beta_m \triangleq \frac{1}{2} \mu_m A_m^2 g_m \hat{g}_m \cos \Delta \theta_{c,m} \quad (9)$$

where $\Delta \theta_{c,m} \triangleq \theta_{c,m} - \hat{\theta}_{c,m}$

Also, using similarity transformation we can convert (8) into the transformed domain as

$$\begin{pmatrix} E[\xi_{I,m}(n+1)] \\ E[\xi_{Q,m}(n+1)] \end{pmatrix} = \begin{pmatrix} 1-\lambda_{I,m} & 0 \\ 0 & 1-\lambda_{Q,m} \end{pmatrix} \begin{pmatrix} E[\xi_{I,m}(n)] \\ E[\xi_{Q,m}(n)] \end{pmatrix} \quad (10)$$

where

$$\lambda_{i,m} = \frac{1}{2} \mu_m A_m^2 g_m \hat{g}_m \{ \cos \Delta \theta_{c,m} \pm j \sin \Delta \theta_{c,m} \} \quad i = I, Q.$$

It should be noted from (10) that since $\lambda_{i,m}$'s are complex values, so are the transformed weight errors. Therefore, we consider the convergence of the magnitude of the transformed error as

$$\rho_{i,m}(n+1) = |1 - \lambda_{i,m}| \rho_{i,m}(n), \quad i = I, Q \quad (11)$$

where $\rho_{i,m}(n) \triangleq |E[\xi_{i,m}(n)]|$.

We can see from (11) that the magnitude converges exponentially to zero (*i.e.*, $E[\omega_{i,m}(n)]$ to $\omega_{i,m}^*$) under the following condition

$$|1 - \lambda_{i,m}| < 1 \quad \forall_i \quad i = I, Q \quad (12)$$

Squaring both sides of (12) yields

$$1 - \mu_m A_m^2 g_m \hat{g}_m \cos \Delta \theta_{c,m} + \frac{1}{4} \mu_m^2 A_m^4 g_m^2 \hat{g}_m^2 < 1$$

$$0 < \mu_m < \frac{4 \cos \Delta \theta_{c,m}}{A_m^2 g_m \hat{g}_m} \quad \text{or} \quad 0 < \alpha_{f,m} < 1 \quad (13)$$

where $\alpha_{f,m} \triangleq \frac{\mu_m A_m^2 g_m \hat{g}_m}{4 \cos \Delta \theta_{c,m}}$.

The time constant of the exponential convergence is derived from the following [4]:

$$e^{-1/\tau_{i,m}} \cong 1 - \frac{1}{\tau_{i,m}}$$

$$= |1 - \lambda_{i,m}| \quad \text{for larg } \tau_{i,m}, \quad i = I, Q \quad (14)$$

From (11) and (14) we get

$$\tau_{i,m} = \frac{1}{1 - \sqrt{1 - \mu_m A_m^2 g_m \hat{g}_m \cos \Delta \theta_{c,m} + \frac{1}{4} \mu_m^2 A_m^4 g_m^2 \hat{g}_m^2}}$$

$$= \frac{1}{1 - \sqrt{1 - 4 \alpha_{f,m} (1 - \alpha_{f,m}) \cos^2 \Delta \theta_{c,m}}} \quad (15)$$

where $i = I$ and Q .

B. The sum of the squared weight errors

Next we investigate the convergence of the mean-square-error (MSE), $E[e^2(n)]$. Using (2), (6) and (8) we can express the MSE as

$$E[e^2(n)] = \sum_{m=1}^M e_m^2(n) + \sigma_\eta^2$$

$$= \frac{1}{2} \sum_{m=1}^M A_m^2 g_m^2 e_m(n) + \sigma_\eta^2 \quad (16)$$

where $\sigma_\eta^2 \triangleq E[\eta^2(n)]$,
 $\xi_m(n) \triangleq E[v_{I,m}^2(n)] + E[v_{Q,m}^2(n)]$.

It is noted from (16) that the convergence study for the MSE is equivalent to that for the sum of the mean-squared weight errors. Inserting (5), (2) and (6) into (4), squaring and taking expectation of both sides of the result yields

$$\xi_m(n+1) = \gamma_m \xi_m(n) + \delta_m \quad (17)$$

where

$$\gamma_m \triangleq 1 - \mu_m A_m^2 g_m \hat{g}_m \cos \Delta \theta_{c,m}$$

$$+ \frac{1}{16} \mu_m^2 A_m^4 g_m^2 \hat{g}_m^2 [9 - \cos(2\Delta \theta_{c,m})],$$

$$\delta_m \triangleq \mu_m^2 A_m^2 g_m^2 \hat{g}_m^2 \sigma_\eta^2.$$

Thus, when $|\gamma| < 1$, (17) has the solution

$$\xi_m(n) = \gamma_m^n \xi_m(0) + \frac{1 - \gamma_m^n}{1 - \gamma_m} \delta_m. \quad (18)$$

Consequently, the convergence condition of the sum of the squared weight errors can be obtained from (18).

$$|\gamma_m| < 1. \quad (19)$$

Solving (19) yields

$$0 < \mu_m < \frac{16 \cos \Delta \theta_{c,m}}{A_m^2 g_m \hat{g}_m (9 - \cos 2\Delta \theta_{c,m})}$$

$$\text{or } 0 < \alpha_{m,s} < 1. \quad (20)$$

where $\alpha_{m,s} \triangleq \mu_m A_m^2 \frac{g_m \hat{g}_m (9 - \cos 2\Delta \theta_{c,m})}{16 \cos \Delta \theta_{c,m}}$.

The time constant of the exponential convergence is derived from (18) and (14).

$$\tau_{m,s} = \frac{1}{\mu_m A_m^2 g_m \hat{g}_m \{ \cos \Delta \theta_{c,m} - \varepsilon \}}$$

$$= \frac{9 - \cos 2\Delta \theta_{c,m}}{16 \alpha_{m,s} (1 - \alpha_{m,s}) \cos^2 \Delta \theta_{c,m}} \quad (21)$$

where

$$\varepsilon \triangleq \frac{1}{16} \mu_m A_m^2 g_m \hat{g}_m (9 - \cos 2\Delta \theta_{c,m}).$$

We can obtain the steady-state value as

$$\xi_m(\infty) = \delta_m / (1 - \gamma_m)$$

$$= \frac{\mu_m \hat{g}_m \sigma_\eta^2}{g_m \{ \cos \Delta \theta_{c,m} - \varepsilon \}}$$

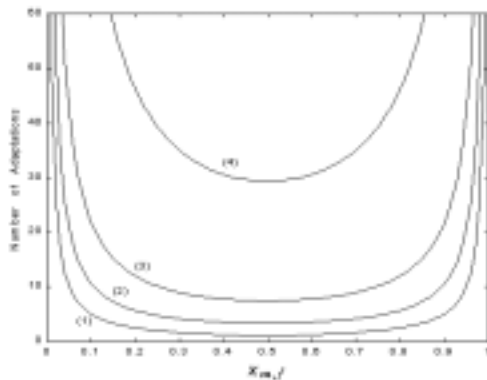
$$= \frac{16 \chi_{m,s} \sigma_n^2}{A_m^2 g_m^2 (1 - \chi_{m,s}) (9 - \cos 2\Delta\theta_{c,m})} \quad (22)$$

The results of the convergence analysis are summarized in Table I.

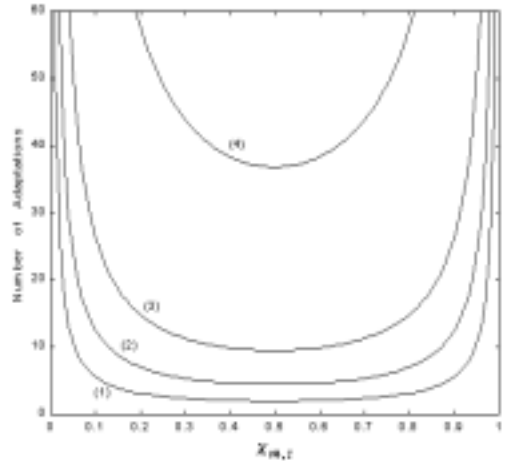
Table I The results of the convergence analysis of the Filtered-x LMS algorithm.

	mean of weight error (Magnitude) $\chi_{m,f} \triangleq \frac{\mu_m A_m^2 g_m \hat{\sigma}_n}{4 \cos \Delta\theta_{c,m}}$	Summed variance of weight errors $\chi_{m,s} \triangleq \frac{\mu_m A_m^2 g_m \hat{\sigma}_n [9 - \cos(2\Delta\theta_{c,m})]}{16 \cos \Delta\theta_{c,m}}$
Stability condition	$0 < \mu_m < \frac{4 \cos \Delta\theta_{c,m}}{A_m^2 g_m \hat{\sigma}_n}$ or $0 < \chi_{m,f} < 1$	$0 < \mu_m < \frac{16 \cos \Delta\theta_{c,m}}{A_m^2 g_m \hat{\sigma}_n [9 - \cos(2\Delta\theta_{c,m})]}$ or $0 < \chi_{m,s} < 1$
Time constant	$\frac{1}{1 - \sqrt{1 - 4\chi_{m,f}(1 - \chi_{m,f})\cos^2 \Delta\theta_{c,m}}}$	$\frac{9 - \cos(2\Delta\theta_{c,m})}{16\chi_{m,s}(1 - \chi_{m,s})\cos^2 \Delta\theta_{c,m}}$
Steady-state value	0	$\frac{16\chi_{m,s} \sigma_n^2}{A_m^2 g_m^2 (1 - \chi_{m,s}) [9 - \cos(2\Delta\theta_{c,m})]}$

Fig. 4 show the time constant curves obtained from the analysis of the mean of the weight error magnitude and the summed variance of weight errors when the phase errors $|\Delta\theta_{c,m}|$ are (1) 0° , (2) 45° , (3) 60° , and (4) 75° . We can see that the convergence speed is the fastest for $\chi_m = 0.5$ in case of same $|\Delta\theta_{c,m}|$.



(a) Mean of the weight error magnitude.



(b) Summed variance of the weight.

Fig. 4. Time constant.

- (1) $|\Delta\theta_{c,m}| = 0^\circ$, (2) $|\Delta\theta_{c,m}| = 45^\circ$,
- (3) $|\Delta\theta_{c,m}| = 60^\circ$, (4) $|\Delta\theta_{c,m}| = 75^\circ$.

IV. SIMULATION RESULTS

Results of computer simulation are presented in this section along with those of the theoretical analysis of the Filtered-x LMS algorithm in section III. For convenience, we consider a single sinusoid case. The input signal $x(n)$ and desired signal $d(n)$ are given as

$$x(n) = \sqrt{2} \left\{ \cos\left(\frac{240\pi n}{2000} + \varphi_1\right) + \cos\left(\frac{480\pi n}{2000} + \varphi_2\right) \right\},$$

$$d(n) = \sum_{l=1}^2 \{ \omega_{l,m}^* x_{l,m}(n) + \omega_{0,m}^* x_{0,m}(n) \} = 0.6x_{l,1}(n) - 0.1x_{0,1}(n) + 0.3x_{l,1}(n) - 0.3x_{0,1}(n). \quad (23)$$

where the sinusoidal frequencies of the sinusoid and sampling were 120 Hz, 240Hz and 2KHz, respectively. The variance of the zero-mean measurement noise was 0.001. The initial weight values were all zero. The simulation results were obtained by ensemble averaging 1000 independent runs. The convergence constant μ was 0.002.

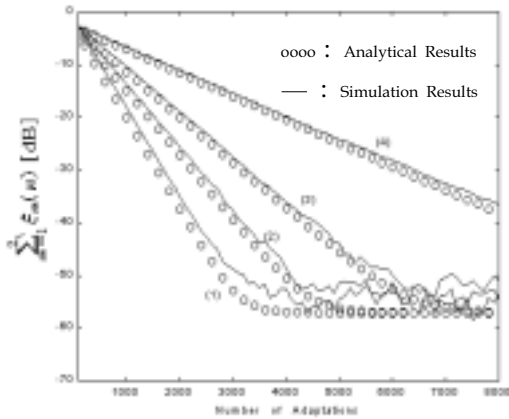


Fig. 5. Learning curves of the summed variance of the weight errors.

- (1) $|\Delta\theta_{c,m}| = 0^\circ$, (2) $|\Delta\theta_{c,m}| = 45^\circ$,
- (3) $|\Delta\theta_{c,m}| = 60^\circ$, (4) $|\Delta\theta_{c,m}| = 75^\circ$.

Fig. 5 show the learning curves obtained from the analysis and simulation of the summed variance of weight errors when the phase errors $|\Delta\theta_{c,m}|$ are (1) 0° , (2) 45° , (3) 60° , and (4) 75° . It can be seen from the figure that the theoretical results for the summed variance behavior agree well with the simulation result. We can also see that the convergence speed is the fastest for $|\Delta\theta_{c,m}| = 0^\circ$.

V. CONCLUSIONS

We can easily see from Table I that the effects of parameter estimation inaccuracy on the convergence behavior of the filtered-x LMS algorithm are characterized by two distinct components : Phase estimation error $\Delta\theta_c$ and estimated magnitude \hat{g} . In particular, $|\Delta\theta_c|$ should be less than 90° for convergence. It is, however, noted that once χ_f or χ_s is selected, the convergence turns out to be determined only by $\Delta\theta_c$. The convergence speed is the fastest for $\chi = 1/2$ regardless of

$\Delta\theta_c$. When $\Delta\theta_c = 0$ and $\hat{g} = g$ the convergence result becomes the same as the LMS case. In conclusion, the convergence of the Filtered-x LMS algorithm is shown to be strongly affected by the accuracy of the phase response estimate.

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rea Institute of Telematics and Electronics, the Korean Institute of Communication Sciences, and the Acoustical Society of Korea.



Kang Seung Lee was born in Korea, in 1962. He received the B.S., M.S., and Ph.D. degree in electronic engineering from Yonsei University, Seoul, Korea, in 1985, 19

91 and 1995, respectively.

From 1991 to 1995, he served as a Research Associate at Yonsei University. From 1987 to 1996, he served as a Senior Member of Research Staff at Korea Electric Power Research Center, Taejeon City. Since 1996, he has been with the Department of Computer Engineering, Donggeui University, Pusan, as an Associate Professor. He also held visiting appointment with the Electrical Engineering Department at Stanford University from 2000 to 2001. His research interests include adaptive digital signal processing, image processing, multimedia signal processing and digital communications.

He is a member of IEEE(the Institute of Electrical and Electronics Engineers), AES(Audio Engineering Society), the Ko